

## TIME TABLE

TIME	Monday June 26	Tuesday June 27	Wednesday June 28	Thursday June 29	Friday June 30
9.00 - 9.45	Registration	Sluckin	Kralj	Biscari	Napoli
9.45 - 10.30	Biscari	Sluckin	Kralj	Biscari	Napoli
11.00 - 11.45	Vergori	Biscari	Sluckin	Vitelli	Vitelli
11.45 - 12.30	Vergori	Biscari	Sluckin	Vitelli	Vitelli
14.00 - 14.45	Sluckin	Vitelli	Biscari	Napoli	
14.45 - 15.30	Sluckin	Vitelli	Vergori	Napoli	
16.00 - 16.45	Kralj	Vergori	Vergori	Kralj	
16.45 - 17.30	Kralj	Vergori	Napoli	Kralj	

## ADMISSION AND ACCOMMODATION

The registration fee is 575.00 Euro + VAT taxes\*, where applicable (bank charges are not included). The registration fee includes a complimentary bag, four fixed menu buffet lunches (on Friday upon request), hot beverages, downloadable lecture notes and wi-fi internet access.

Applicants must apply at least one month before the beginning of the course. Application forms should be sent on-line through our web site: <http://www.cism.it>. A message of confirmation will be sent to accepted participants. If you need assistance for registration please contact our secretariat.

Applicants may cancel their course registration and receive a full refund by notifying CISM Secretariat in writing (by email) no later than two weeks prior to the start of the course.

If cancellation occurs less than two weeks prior to the start of the course, a Euro 50.00 handling fee will be charged. Incorrect payments are subject to Euro 50.00 handling fee.

A limited number of participants from universities and research centres who are not supported by their own institutions can be offered board and/or lodging in a reasonably priced hotel or student dormitory, if available.

Requests should be sent to CISM Secretariat by **April 26, 2017** along with the applicant's curriculum and a letter of recommendation by the head of the department or a supervisor confirming that the institute cannot provide funding. Preference will be given to applicants from countries that sponsor CISM.

Information about travel and accommodation is available on our web site, or can be mailed upon request.

\* Italian VAT is 22%.

*For further information please contact:*

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# CONTINUUM MECHANICS AND PHYSICS OF LIQUID CRYSTALS

Advanced School  
 coordinated by

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 Italy

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 University of Glasgow  
 UK

**Udine June 26 - 30 2017**

## CONTINUUM MECHANICS AND PHYSICS OF LIQUID CRYSTALS

Liquid crystals (LCs) are matter in a state that exhibits intermediate physical properties between those of conventional liquids and those of solid crystals: they may flow like a liquid, but their molecules may be oriented along a common direction like in a crystal. The particular shape of LCs renders the molecules very sensitive to the presence of physical boundaries and to the action of magnetic or electric fields. Depending on the magnetic properties of the LC, molecules may reorient along, or normally to, the direction of the field. In particular, the sudden application of a field switches on/off the transmission of polarized light. Thus, LCs may find wide applications in computer monitors, flat-panel televisions, cell phones, calculators and watches. The classical mathematical

theory of LCs (that concerns only statics) is a continuum theory based on the pioneer works by Oseen (1933), Zocher (1933) and Frank (1958). The continuum dynamical theory is instead due to the independent contributions by Ericksen (1962) and Leslie (1968). These theories use a single order parameter, called the director, a unit vector pointing along the average microscopic molecular orientation. Many phenomena in LCs fit well within the classical description. However, the transition from ordered to disordered states escapes the director theory. The classical microscopic description of defects and surface phenomena yields undesired results as well. The more recent order-tensor theory put forward by de Gennes (Nobel Prize laureate in physics in 1991) in two works (dated

1969 and 1971) focuses on the orientational probability distribution, and introduces the measures of the degree of orientation and biaxiality. This theory was reformulated rigorously by Ericksen (1991). Recent studies have shown the inadequacy of classical continuum theories to study:

- the geometry and topology of active liquid crystals under confinement,
- the mechanics of ultra-thin nematics deposited on curved substrates (nematic shells),
- the anisotropic elasticity and dynamic relaxation of LCs.

On the contrary, these phenomena can be studied by means of suitable generalizations or adaptations of existing classical models or thanks to novel more complex theories. The course aims at providing carefully crafted overviews of

classical and novel continuum theories for LCs to study topological defects, equilibrium textures, active flows and acoustic wave propagation. The lectures will include surveys of relevant differential geometry and analytical methods that are essential to a proper understanding, in addition to overviews on the mathematical modelling of the subject from various perspectives. Representing a "tour d'horizon" on the physics of LCs, the presentations will highlight the efficiency of continuum theories in modelling real world phenomena. The course is addressed to doctoral students, post-doctoral researchers and academics interested in the use of continuum mechanics to model, analyse and understand the physics and mechanics of liquid crystals.

## PRELIMINARY SUGGESTED READINGS

Manfredo P. do Carmo. *Differential Geometry of Curves and Surfaces*. Prentice-Hall, Englewood Cliffs, NJ, 1976.

T. Lopez-Leon, V. Koning, K. B. S. Devaiah, V. Vitelli, and A. A. Fernandez-Nieves. Frustrated nematic order in spherical geometries. *Nat Phys*, 7(5):391–394, 5 2011.

M. C. Marchetti, J. F. Joanny, S. Ramaswamy, T. B. Liverpool, J. Prost, Madan Rao, and R. Aditi Simha. Hydrodynamics of soft active matter. *Reviews of Modern Physics*, 85(3):1143–1189, 2013.

G Napoli and L Vergori. Extrinsic curvature effects on nematic shells. *Phys. Rev. Lett.*, 108(20):207803–, 05 2012.

I. W. Stewart. *The static and dynamic continuum theory of liquid crystals: a mathematical introduction*. Taylor & Francis, London and New York, 2004.

E G Virga. *Variational Theories For Liquid Crystals Variational Theories For Liquid Crystals*. Chapman-Hall, London, 1994.

## LECTURES

All lectures will be given in English. Lecture notes can be downloaded from the CISM web site. Instructions will be sent to accepted participants.

## INVITED LECTURERS

**Paolo Biscari** - Politecnico di Milano, Milano, Italy  
*6 lectures on:* Relaxational dynamics of nematic liquid crystals. In this course we explore a novel hydrodynamic theory which includes both anisotropic elasticity and dynamic relaxation. Liquid remodelling is encompassed through a continuous update of the shear-stress free configuration. The theory will be then specialized to analyse the hydrodynamic response of nematic liquid crystals.

**Samo Kralj** - FNM, University of Maribor, Maribor, Slovenia  
*6 lectures on:* Topological defects in 2D nematic films: electrostatic analogy. A study of topological defects within effectively two-dimensional (2D) liquid crystal films exhibiting in-plane orientational ordering will be presented. Popular examples of such class of systems are liquid crystalline shells and various biological membranes. The model free energy in terms of nematic tensor order parameter and curvature tensor will be introduced. It will be also demonstrated how different shapes of closed films could be obtained experimentally.

**Gaetano Napoli** - Università del Salento, Lecce, Italy  
*5 lectures on:* Surface free energies for liquid crystalline shells. The course focuses on models for the free energy density of two-dimensional liquid crystals lying on curved substrates. Both director and tensor order theories will be presented. We will discuss the influence of the curvature of the substrate on the alignment of the molecules.

**Tim Sluckin** - University of Southampton, Southampton, UK  
*6 lectures on:* Biaxial nematic liquid crystals: Biaxial nematics have their molecules differentially oriented along two axes. The course focuses on mean field theories on biaxial phases and their implications on order parameters and phase transitions.

**Luigi Vergori** - University of Glasgow, Glasgow, UK  
*6 lectures on:* Differential geometry of nematic shells. Brief description: The course aims at introducing the basic results in the differential geometry of nematic shells. The results presented are essential to the derivation of models for the free energy density of thin liquid crystalline films.

**Vincenzo Vitelli** - Institut-Lorentz for Theoretical Physics, Leiden University, The Netherlands.  
*6 lectures on:* Geometry and topology of active liquid crystals under confinement. The course will cover the geometry and topology of active liquid crystals under confinement. First we will discuss how the shape of a micro channel can influence active flow. Second we will review the topological features of the excitations and explore connections with the physics of topological insulators.