

TIME TABLE

TIME	Monday September 7	Tuesday September 8	Wednesday September 9	Thursday September 10	Friday September 11
9.00 - 9.45	Registration	Bluman	Bluman	Bluman	Bluman
9.45 - 10.30	Bluman	Ganghoffer	Ganghoffer	Ganghoffer	Ganghoffer
11.00 - 11.45	Ganghoffer	Müller	Müller	Müller	Müller
11.45 - 12.30	Müller	Oberlack	Slawianowski	Oberlack	Mladenov
14.00 - 14.45	Bluman	Ganghoffer	Müller	Slawianowski	
14.45 - 15.30	Oberlack	Oberlack	Oberlack	Oberlack	
16.00 - 16.45	Slawianowski	Slawianowski	Slawianowski	Slawianowski	
16.45 - 17.30	Mladenov	Mladenov	Mladenov	Mladenov	

ADMISSION AND ACCOMMODATION

The registration fee is of 575,00 Euro + VAT taxes*, where applicable (bank charges are not included).

The registration fee includes a complimentary bag, four fixed menu buffet lunches (Friday subject to numbers), hot beverages, downloadable lecture notes and wi-fi internet access.

Applicants must apply at least one month before the beginning of the course. Application forms should be sent on-line through our web site: <http://www.cism.it> or by post.

A message of confirmation will be sent to accepted participants. If you need assistance for registration please contact our secretariat.

Applicants may cancel their course registration and receive a full refund by notifying CISM Secretariat in writing (by email) no later than two weeks prior to the start of the course.

If cancellation occurs less than two weeks prior to the start of the course, a Euro 50,00 handling fee will be charged. Incorrect payments are subject to Euro 50,00 handling fee.

A limited number of participants from universities and research centres who are not supported by their own institutions can be offered board and/or lodging in a reasonably priced hotel or students' dormitories, if available.

Requests should be sent to CISM Secretariat by **July 7, 2015** along with the applicant's curriculum and a letter of recommendation by the head of the department or a supervisor confirming that the institute cannot provide funding. Preference will be given to applicants from countries that sponsor CISM.

Information about travel and accommodation is available on our web site, or can be mailed upon request.

Please note that the Centre will be closed for summer vacation the first three weeks in August.

* Italian VAT is 22%.

For further information please contact:

CISM
 Palazzo del Torso
 Piazza Garibaldi 18
 33100 Udine (Italy)
 tel. +39 0432 248511 (6 lines)
 fax +39 0432 248550
 e-mail: cism@cism.it



SIMILARITY, SYMMETRY AND GROUP THEORETICAL METHODS IN MECHANICS

Advanced School
coordinated by

Jean-François Ganghoffer
 Université de Lorraine
 Nancy, France

Ivailo Mladenov
 Bulgarian Academy of Sciences
 Sofia, Bulgaria

Udine September 7 - 11 2015

SIMILARITY, SYMMETRY AND GROUP THEORETICAL METHODS IN MECHANICS

The aim of the course is to bring together researchers in mechanics, applied physics and applied mathematics who use similarity and symmetry analysis of engineering problems in both solid and fluid mechanics, researchers who are developing significant extensions of these methods implement, and numerical analysts who develop and use such methods in numerical schemes. The powerfulness of the Lie group symmetry analysis has been extensively utilized, essentially to support the finding of analytic solutions to partial differential equations. For a given DE problem, one can algorithmically calculate its admitted point symmetries – transformations of dependent and independent variables that map a problem into itself. Knowledge of admitted symmetries allows one to construct mappings relating DE systems, find out whether or not a given nonlinear DE system can be mapped into a linear system by an invertible transformation, and find exact (group-invariant or symmetry-generated) solutions. Lie group analysis is of further interest in setting up numerical schemes preserving the group properties of an initial boundary value problem (BVP).

Symmetries have been historically relied upon to construct Lagrangian formulations in field theory. In the context of continuum solids mechanics, Lie groups have been applied to solve the Navier and the Lamé equations, or, in a similar spirit and extending this view to dissipation, to partially solve the ideal plasticity equation, to formulate conservation laws and invariance relations, to analyze the kinematics of mechanisms, and more recently to formulate the constitutive laws and master response of materials with complex rheological behaviors. Symmetry methods have a fundamental role in Lagrangian mechanics, Eshelbian mechanics, and nonlinear elasticity. The field of Eshelbian Mechanics (so called in the honor of the works of Eshelby, but also known as Configurational Mechanics), relies on translational symmetries in the material space, for writing field equations in terms of Eshelby stresses. Those symmetries extended to rotations and dilatations have been intensively used to construct the well known J-integrals. The concept of nonlocal symmetries allows to construct novel BVP in continuum mechanics (and group invariant solutions), involving potential variables, thereby extending

the classical picture relying on the traditional Lagrangian and Eulerian viewpoints. Symmetry methods are at the basis of methodologies for finding invariance relations of the BVP of continua obeying non dissipative and dissipative behaviors, including nonlinear elasticity, plasticity and creep. Lie symmetries are useful to find conservation laws in the analysis of Euler and Navier-Stokes equations for incompressible fluids: this particularly includes very recent results on new vorticity related conservation laws for Euler and Navier-Stokes equations and others which only exist in reduced dimensions such for as for plan or helically symmetric flows. The three “complete approaches” to statistical turbulence theory are an immediate consequence of Navier-Stokes equations. Beside the classical Lie symmetries stemming from Navier-Stokes equations, these sets of equations admit more Lie symmetries, named statistical symmetries. The involvement of Lie groups as a new predictive and systematic methodology to obtain invariance properties of materials is more recent. From the knowledge of the constitutive law of a given material, Lie symmetries are able to predict

its response under various control conditions, and inversely to formulate a material's constitutive law exploiting a postulated Lie group structure satisfying the symmetries involved in the experimental data. The proposed course will reflect the organization of the Summer School on the same topics that took place in Varna, Bulgaria (June 7-12, 2013), jointly organized by I. Mladenov and J.F. Ganghoffer. Those topics were dealt with by three main speakers, leaders in the field, who made a pedagogical introduction and laid out key issues and concepts: G. Bluman (UBC, Vancouver, Canada), N. Ibragimov (Blekinge Institute of Technology, Karlskrona University, Sweden), and C-M. Marle (Univ. Pierre et Marie Curie and French Academy of Sciences, Paris). Two of these lecturers will deliver courses during the CISM session. The course is mostly intended for Master students in mechanics or applied mathematics (or in physics, but having a sufficiently good level in mechanics, defined by the prerequisites), for PHD students, post-doctoral students, industrial researchers and engineers interested in the more practical use of symmetry methods. Permanent researchers willing to get an overview of the field are also welcome.

INVITED LECTURERS

George Bluman - University of British Columbia, Vancouver, Canada
6 lectures on: [These five lectures will give an overview of recent developments by George Bluman and his collaborators in the field of symmetries and differential equations.](#) •General introduction giving an extensive overview of topics to be covered. •Review of local symmetries - point, contact, higher-order. •Construction of conservation laws (CLs) - direct method to find them, connections with Noether's theorem. •Use of symmetries to construct new conservation laws from known CLs. •How to systematically find trees of equivalent but nonlocally related PDE systems for a given PDE system through the use of CLs, point symmetries and subsystems. •How to systematically find nonlocal symmetries and nonlocal conservation laws for a given PDE system. •The multidimensional situation. •All topics will be illustrated through numerous examples.

Jean-François Ganghoffer - Université de Lorraine, Nancy, France
6 lectures on: [Symmetry methods in continuum solid mechanics of materials.](#) •Symmetries in the Lagrangian formulation of field theories. •Symmetries in continuum solid mechanics (nonlinear elasticity). •Invariance relations in nonlinear elasticity, path independent integrals. •Eshelbian mechanics. •Applications of Lie symmetries in elastoviscoplasticity: construction of invariance relations and master responses.

Ivailo Mladenov - Bulgarian Academy of Sciences, Sofia, Bulgaria
5 lectures on: [The Many Faces of Elastica.](#) •Geometrical background. •Intrinsic equations. •Symmetries. The generalized elastica. •Membrane shapes, Hele-Shaw cells. •Explicit solutions of the shape equation.

Andreas Müller - Shanghai Jiao Tong University Joint Institute, China
6 lectures on: [Group Theoretical Approaches to the Mobility and Singularities of Mechanisms.](#) •Analytic varieties and mobility concepts. •Non-smooth kinematic phenomena. •Higher-order local analysis. •Generic statements. •Open problems and alternative routes.

Jan J. Slawianowski - University of Warsaw, Poland
6 lectures on: [Mechanical Systems with Affine and Unitary Degrees of Freedom.](#) •Hamiltonian and quantum systems on Lie groups and homogeneous spaces. •Rigid body and affinely-rigid body. •Affinely-invariant dynamics of affinely-rigid body. •Micromorphic mechanics and its affine generalization. •Born-Infeld theory and the mechanics of shells. •D'Alembert and Vakonomic variational principles.

Martin Oberlack - Technical University, Darmstadt, Germany
6 lectures on: [Symmetry Methods in Fluid Mechanics and Turbulence Theory.](#) •Symmetries of Euler and Navier-Stokes equations in 3D. •Conservation laws of Euler and Navier-Stokes equations in 3D. •Symmetries and conservation laws of Euler and Navier-Stokes equations in reduced dimensions. •The three fundamental statistical approaches to turbulence: Lundgren-Monin-Novikov pdf equations, the Friedmann-Keller moment equations and the Hopf functional equation. •Counterpart of classical symmetries of Euler and Navier-Stokes for turbulence statistics. •New statistical symmetries of turbulence with no classical counterpart. •Symmetry invariant solutions as turbulent scaling laws derived from classical and new statistical symmetries.

LECTURES

All lectures will be given in English. Lecture notes can be downloaded from the CISM web site, instructions will be sent to accepted participants.

PRELIMINARY SUGGESTED READINGS

G. Bluman, A. Cheviakov, S. Anco. Applications of Symmetry Methods to Partial Differential Equations, Appl. Math. Sci. vol. 168, Springer, New York 2010, 417pp.

G. Bluman, A. Cheviakov, J.F. Ganghoffer. 'Nonlocally related PDE systems for one-dimensional nonlinear elastodynamics'. Int. J. Engng Math. 2008. DOI 10.1007/s10665-008-9221-7.

V. Magnenet, R. Rahouadj, J.F. Ganghoffer, C. Cunat. Continuous symmetries and constitutive laws of thermo-elasto(visco)plastic materials

within a thermodynamical framework of relaxation. Part I: formal aspects. Int. J. Plasticity, 23, Issue 1, 2007, 87-113.

A. Cheviakov, J.F. Ganghoffer. Symmetry Properties of Two-Dimensional Ciarlet-Mooney-Rivlin Constitutive Models in Nonlinear Elastodynamics. Journal of Mathematical Analysis and Applications. 2012. 396, 625–639.

J.F. Ganghoffer, V. Magnenet, R. Rahouadj. Relevance of symmetry methods in mechanics of materials. Int. J. Engng Math., 66, 103-119, 2010.

I. Mladenov, New Solutions of the Shape Equation, Eur. Phys. J. B 29, 327-330, 2002.

A. Müller, J. Rico: Mobility and Higher Order Local Analysis of the Mechanisms, in: J. Lenarcic, P. Wenger (eds.), Advances in Robot Kinematics, 2008, Springer, pp. 215-224.

A. Müller: On the Manifold Property of the Set of Singularities of Kinematic Mappings: Modeling, Classification, and Genericity, ASME Trans., Journal of Mechanisms and Robotics, vol. 3, 2011.

J.J. Slawianowski. Geometry of Phase Spaces. Wiley & Sons, 1991.

J. J. Slawianowski. The Mechanics of the Homogeneously Deformable Body. Dynamical Models with High Symmetries. Zeitschrift für angewandte Mathematik und Mechanik 62: 229 – 240, 2006. doi:10.1002/zamm.19820620604.

V. Vassilev, I.M. Mladenov, Geometric Symmetry Groups, Conservation Laws and Group-Invariant Solutions of the Willmore Equation, Geometry, Integrability and Quantization 5, 246-265, 2004.

**SIMILARITY, SYMMETRY AND GROUP
THEORETICAL METHODS IN MECHANICS**

Udine, September 7 - 11, 2015

Application Form
(Please print or type)

Surname _____

Name _____

Affiliation _____

Address _____

E-mail _____

Phone _____ Fax _____

Method of payment upon receipt of confirmation (Please check the box)

The fee is 575,00 Euro + 22% Italian VAT taxes, where applicable (bank charges are not included).

I shall send a check of Euro _____

Payment will be made to CISM - Bank Account No. 094570210900,
VENETO BANCA - Udine (CAB 12300 - ABI 05035 - SWIFT/BIC
VEBHIT2M - IBAN CODE IT46 N 05035 12300 09457 0210900).
Copy of the receipt should be sent to the secretariat

I shall pay at the registration counter with check or VISA Credit Card
(Mastercard/Eurocard, Visa, CartaSi)

**IMPORTANT: CISM is obliged to present an invoice for the above sum.
Please indicate to whom the invoice should be addressed.**

Name _____

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(* Only for EU residents or foreigners with a permanent business activity in Italy.)

Only for Italian Public Companies

I ask for IVA exemption (ex law n. 537/1993 - art. 14 comma 10).

Privacy policy: I understand that data received via this form will be used only to provide information about CISM and its activities, within the limits set by the Italian legislative decree no. 196/2003 and subsequent amendments.

Complete information on CISM's privacy policy is available at www.cism.it.

I have read the "Admission and Accommodation" terms and conditions and agree.

Date _____ Signature _____